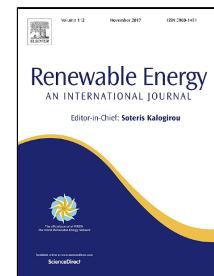


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Optimal Management of Renewable Energy Sources by Virtual Power Plant

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1 Optimal Management of Renewable Energy Sources by

2 Virtual Power Plant

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10
11 **Abstract-** In recent years, due to lack of sufficient quantity of fossil fuel, the need of Renewable
12 Energy Sources (RESs) has become an important matter. In addition to the shortage of fossil fuel,
13 global warming is another concern for many countries and companies. These issues have caused a
14 large number of RESs to be added into modern distribution systems. Nevertheless, the high
15 penetration of RESs beside the intermittent nature of some resources such as Wind Turbines (WT)
16 and Photovoltaic (PV) cause the variable generation and uncertainty in power system. Under this
17 condition, an idea to solve problems due to the variable outputs of these resources is to aggregate
18 them together. A collection of Distributed Generators (DGs), Energy Storage Systems (ESSs) and
19 controllable loads that are aggregated and then are managed by an Energy Management System
20 (EMS) which is called Virtual Power Plant (VPP). The objective of the VPP in this paper is to
21 minimize the total operating cost, considering energy loss cost in a 24h time interval. To solve the
22 problem, Imperialist Competitive Algorithm (ICA), a meta-heuristic optimization algorithm is
23 proposed to determine optimal energy management of a VPP with RESs, Battery Energy Storage
24 (BSS) and load control in a case study.

25
26 **Keywords:** Virtual power plant, Renewable energy sources, Optimal energy management,
27 Operating cost, Imperialist competitive algorithm.

28 1. Introduction

29
30 In recent years, major advances in the technology of DGs such as solar, wind, hydro and etc. have
31 led them to be in the center of consideration more than before, because of need for lower cost, less
32 environmental pollution, more flexibility, higher reliability, and better power quality. On the other
33 hand, due to lack of fossil fuel that leads to increase in energy prices and the gradual rise in the
34 global temperature, many industrialized countries have been compelled to alter the focus of their
35 energy policy towards different kinds of energy supplies and deployment of RESs. Since RESs
36 cannot yet supply levels of return on investment similarly to fossil fuels [1], various encouraging
37 plans for RES have been initiated. These contain discount in tariff plan, discount in premium plan
38 and the quota plan. Due to this fact, wind power and photovoltaic are considered more than other
39 sources. In the year 2015, the worldwide wind power capacity reached 433 GW with an annual
40 growth rate of 15% [2], while the installed solar photovoltaic (PV) in the same year reached a
41 cumulative capacity of 233 GW, with an annual growth rate over 30% [3]. For a large number of
42 RESs, it is troublesome to control their output, mainly when the output of the generators such as
43 wind power and photovoltaic fluctuate quickly and are intermittent. A solution to this problem is to
44 aggregate the RESs, so that they emerge generally like a conventional generator with relatively
45 stable output. One of the aggregation approaches is to create a VPP.

46
47 VPP is a combination of renewable sources, Energy Storage System (ESS), small conventional
48 power plants and interruptible loads that can supply market actions as a single power plant [4].
49 However, Hybrid systems in different locations of any country could be controlled by a VPP. In

50 order to participate in the VPP structure and provide a virtual hybrid system, there is an aggregator
 51 that makes contracts with each DG owner. Thus, the aggregator acquires the chance of contributing
 52 in the electricity market with a reliable power quality. Because of the uncertainty and intermittent
 53 nature of PV and WT powers, it is usually possible that the actual values of these variables are
 54 different from the corresponding schemed values. Therefore, grid operators attempt to have a
 55 definite level of reserve in the grid. Thus, they would be capable of compensating for the
 56 uncertainty in the output power of these sources to protect the system security [5-6]. In order to
 57 compensate the uncertainty of wind and PV powers, Pumped Hydro Energy Storage (PHES),
 58 Compressed Air Energy Storage (CAES), flywheel energy storage, Super conducting Magnetic
 59 Energy Storage (SMES), super capacitor energy storage and battery energy storage are used [7]. The
 60 storage units have two major benefits: first, these are loads with limited abilities, and second they
 61 can turn into generators. Nowadays, many papers have concentrated on VPP and different
 62 associated aspects and concept of their interactions with the power system. In [8-9] the VPP is
 63 considered as a centralized entity, including some micro Combined Heat and Power (CHP) units
 64 connected to a low voltage distribution system. An optimal operation approach of a VPP composed
 65 of CHP units is offered based on a decentralized control strategy [10]. In [8-10], however, the
 66 optimal utilization of CHP units has been specified as the main aim but the important role of
 67 electrical storages and demand response resources was not considered. The impact of demand
 68 response on power system operation is assessed in [11]. In [12], a robust optimization tool is
 69 demonstrated by self-scheduling of VPPs with power markets uncertainty. A method for utilization
 70 of the thermal mass of a building to defer power consumption from electric space heating using of
 71 interruptible load in the distribution system is presented in [13]. In [14] optimum operation of a
 72 wind-hydro VPP considering the day-ahead scheduling of VPP components using mixed integer
 73 linear programming (MILP) is presented. In the mentioned study, the energy prices of market and
 74 the deviations of wind power were considered with a risk strategy on bidding prices. In [15], a
 75 control method of VPP, which includes photovoltaic panels and controllable loads, is solved by
 76 using a mixed integer programming so that the power output of the VPP can be set in a wide range
 77 flexibly. In [16], the VPP attempts to maximize its expected turn over via participating in both the
 78 day-ahead and the balancing markets using a two-stage stochastic mixed integer linear programming
 79 model. A heuristic game theory based virtual power market model for security restricted unit
 80 commitment strategy was proposed in [17]. A price-based unit commitment method allowing a VPP
 81 to exchange energy with upstream network for day-ahead market sale/purchase bids was employed
 82 in [18]. In [19] an optimal scheduling of a micro grid, including PV, WT, Fuel cell (FC) in an
 83 isolated load area has been formulated for a 24-hour period and 1h time interval each. Likewise, in
 84 [20] the scheduling of DERs in an isolated grid has been investigated that the optimization problem
 85 has been solved by Branch and Bound technique and then used by an Artificial Neural Network
 86 (ANN) to better manage the DER. In [21], an optimization algorithm is used to solve bi-level
 87 optimal dispatch in VPP considering the uncertain factors number. A methodology is considered in
 88 [22] to control the emissions from a group of generation sources installed in laboratories aggregated
 89 in a VPP. In [23], a combined wind and pumped storage VPP is presented in an island system. In
 90 [24] the weekly scheming of a VPP comprising of intermittent renewable sources, energy storage
 91 device and a conventional power plant for maximizing their total profit is considered. In [25-26] a
 92 VPP bidding strategy in an unbalanced model based on price-based unit commitment is presented to
 93 contribute in energy and spinning reserve markets. In [27], an energy management method is
 94 investigated for VPPs and the cost and emission impacts of VPPs formation and electric vehicle
 95 penetration are analyzed. In [28], a modified particle swarm optimization method has been specified
 96 aiming at minimization of VPP costs in the day-ahead. A new algorithm has been suggested in [29]
 97 in order to optimize electrical and thermal scheduling of a large scale VPP, including cogeneration
 98 systems and energy storage systems, but no specific model for RESs and their corresponding
 99 uncertainties has been proposed.

100 In this paper one probabilistic methodology based on 2m Point Estimate Method (PEM) is proposed
 101 to consider the uncertainties of hourly load demand, available output power of solar and wind and

102 market price. The VPP, which is considered here includes different renewable energy sources such
 103 as wind turbine (WT), photovoltaic (PV), micro turbine (MT), fuel cell (FC) and a battery as storage
 104 device. The objective function of the problem is modeled as the total operating cost of the VPP
 105 considering energy loss cost that is optimized for 24h time period. The optimal operation problem is
 106 modeled as an optimization problem and it is solved by using Imperialist Competitive Algorithm
 107 (ICA) under technical constraints.

108 The rest of the paper is organized as follows: In Section 2, the definition of VPP is presented. In
 109 Sections 3, the objective function and the related constraints are discussed. In Section 4, the 2m
 110 PEM is proposed as an approach to model the uncertainties. In Section 5, the ICA is introduced and
 111 explained completely as an optimization method. In Section 6, the simulation results and
 112 comparison of different methods are shown. Finally, the conclusion is presented in Section 7.

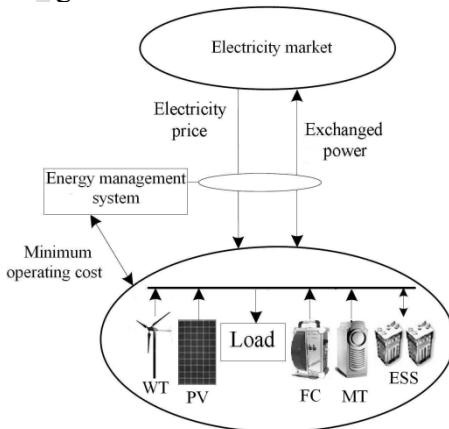
113

114 2. Virtual power plant

115

116 VPP is a combination of dispersed generator units, controllable load and ESS, participating at power
 117 market as an independent power plant for the purpose of trading their electrical energy for
 118 minimizing the cost. When the electricity price in the power market is low, the VPP can buy power
 119 for the power market and charge power into the energy storage systems. But when the electricity
 120 price in the power market is high, the VPP decreases the power obtained from the controlled load
 121 and discharge power from the energy storage systems. The generators of VPP could use fossil fuels
 122 and renewable energy sources. The EMS is the core of the VPP, and it coordinates the output energy
 123 of all generators, the energy storage system's capacity, and the load demand. The VPP concept and
 124 its possibility in the system operation have been identified in some recent researches.

125 The generators that are used in distributed systems are generally based on RES and have a low
 126 output power. Because of the fluctuating power of some RESs such as wind turbine and
 127 photovoltaic, accurate forecast of both the capacity and the moment in which the energy will be
 128 generated, is not straightforward. For that reason, such generators cannot be appropriate in
 129 deregulated power systems for two reasons, first they are not able to suggest the bids for effective
 130 capacity, and second they do not receive the grid requirements for maintaining the systems security.
 131 Such economical and security constraints can be done if these generators are place together to create
 132 a VPP structure. One of the principal features of a VPP is that each part of the VPP is linked directly
 133 to the EMS, so that the central control unit can get their latest status data. Hence, it is important to
 134 provide the connection among units. The aim of the EMS is trading electrical energy with the main
 135 grid and electricity market to achieve energy balance between generation and consumption for
 136 minimizing the operating cost at different hours of the day. The VPP components and interaction
 137 with power market are shown in Fig. 1.



138
 139 **Fig. 1.** VPP and trading of electrical energy with electricity market.
 140
 141
 142

143 **3. Problem formulation**

144
 145 The objective function and the corresponding constraints of the optimal operation management are
 146 described in this section.

147
 148 **3.1. Objective function**
 149

150 This paper presents an energy management scheme in a VPP including renewable and conventional
 151 DGs. The objective function is to minimize the VPP operational cost by the control of the local
 152 production as well as the interactive relationship with the grid. In fact, the VPP will try to supply its
 153 consumers locally. However, if the total power produced by DGs is not enough or too expensive to
 154 cover the supplying loads, then energy is bought from the grid (as the upstream network) and will be
 155 sold to the consumers or stored in the storage devices. Consequently, it can be concluded that the
 156 objective cost consists of the power that exchange between the VPP and grid, the fuel cost for DGs,
 157 and the start up or shut down cost of the power sources used in the VPP. The objective function is
 158 similar to [30], but the principal difference is the cost of the energy loss reduction occurred into
 159 distribution system lines.

160 This function is stated as follows:

161

$$162 \quad \left[\begin{array}{l} P_{Grid}(t) \times C_{Grid}(t) \\ + U_{WT}(t) \times P_{WT}(t) \times C_{WT}(t) \\ + U_{PV}(t) \times P_{PV}(t) \times C_{PV}(t) \\ + U_{FC}(t) \times P_{FC}(t) \times C_{FC}(t) \\ + U_{MT}(t) \times P_{MT}(t) \times C_{MT}(t) \\ \\ Min f = \sum_{t=1}^T Cost = \sum_{t=1}^T \left[\sum_{j=1}^{N_g} U_j(t) \times P_{Sj}(t) \times C_j(t) \right. \\ \left. + \sum_{i=1}^{N_g} S_{Gi} |U_i(t) - U_i(t-1)| \right. \\ \left. + \sum_{j=1}^{N_s} S_{Sj} |U_j(t) - U_j(t-1)| \right. \\ \left. - \Delta P(t) \times C_{\Delta P}(t) \right] \end{array} \right] \quad (1)$$

163
 164
$$165 \quad \sum_{t=1}^T \Delta P(t) = \sum_{t=1}^T (P_{original losses}(t) - P_{new losses}(t)) \quad (2)$$

166
$$167 \quad P_{final losses}(t) = \sum_{t=1}^T \sum_{i=1}^{N_{br}} R_i \times |I_i(t)|^2 \quad (3)$$

168 Where $C_{WT}(t)$, $C_{PV}(t)$, $C_{FC}(t)$, $C_{MT}(t)$ and $C_j(t)$ are the bids of the wind turbine, photovoltaic, fuel cell,
 169 micro turbine and storage devices at hour t respectively. $S_{Gi}(t)$ and $S_{Sj}(t)$ are the start-up or shut-
 170 down costs for i th DG and j th storage respectively, $P_{Grid}(t)$ is the active power which is bought
 171 (sold) from (to) the utility at time t and $C_{Grid}(t)$ is the bid of utility at time t. N_g and N_s represent
 172 the total number of generation and storage units respectively, $U_{WT}(t)$, $U_{PV}(t)$, $U_{FC}(t)$, $U_{MT}(t)$ and
 173 $U_j(t)$ represent the ON or OFF states of all units at hour t of the day. Also $\Delta P(t)$, $C_{\Delta P}(t)$, R_i and I_i are
 174 the difference between the original losses and the new losses of feeders and it's cost at hour t and the
 175 resistance and the actual current of the i^{th} branch respectively [31].

176
 177
 178
 179

180 **3.2. Constraints**
181182 • Power Balance in each time period t
183

184
$$\sum_{t=1}^T \begin{pmatrix} P_{Grid}(t) + P_{WT}(t) \\ + P_{PV}(t) + P_{FC}(t) \\ + P_{Battery\ discharge}(t) \end{pmatrix} = \sum_{t=1}^T \begin{pmatrix} Load(t) \\ + P_{Battery\ charge}(t) \\ + P_{Loss}(t) \end{pmatrix} \quad (4)$$

185

186

187 • Wind turbine generation limitation in each time period t
188

189
$$P_{WT\ min}(t) \leq P_{WT}(t) \leq P_{WT\ max}(t); \quad t = 1, \dots, T \quad (5)$$

190

191 • Photovoltaic generation limitation in each time period t
192

193
$$P_{PV\ min}(t) \leq P_{PV}(t) \leq P_{PV\ max}(t); \quad t = 1, \dots, T \quad (6)$$

194

195 • Fuel cell limitation in each time period t
196

197
$$P_{FC\ min}(t) \leq P_{FC}(t) \leq P_{FC\ max}(t); \quad t = 1, \dots, T \quad (7)$$

198

199 • Micro turbine limitation in each time period t
200

201
$$P_{MT\ min}(t) \leq P_{MT}(t) \leq P_{MT\ max}(t); \quad t = 1, \dots, T \quad (8)$$

202

203 • Utility limitation in each time period t
204

205
$$P_{Grid\ min}(t) \leq P_{Grid}(t) \leq P_{Grid\ max}(t); \quad t = 1, \dots, T \quad (9)$$

206

207 • Storage battery limitation in each time period t
208

209
$$P_{Sj\ min}(t) \leq P_{Sj}(t) \leq P_{Sj\ max}(t); \quad t = 1, \dots, T \quad (10)$$

210

211 Due to restriction on charge and discharge rate of storage devices during each time period the
212 following equation and constraints can be considered:
213

214
$$W_{ess}(t) = W_{ess}(t-1) + \eta_{charge} P_{charge} \Delta t - \frac{1}{\eta_{discharge}} P_{discharge} \Delta t \quad (11)$$

215

216
$$W_{ess\ min} \leq W_{ess}(t) \leq W_{ess\ max}; \quad t = 1, \dots, T \quad (12)$$

217

218
$$P_{charge}(t) \leq P_{charge\ max} \cdot X(t); \quad t = 1, \dots, T; \quad X \in \{0,1\} \quad (13)$$

219

220
$$P_{discharge}(t) \leq P_{discharge\ max} \cdot Y(t); \quad t = 1, \dots, T; \quad Y \in \{0,1\} \quad (14)$$

221

222 • Storage battery cannot charge and discharge at the identical time
223

224
$$X(t) + Y(t) \leq 1; \quad t = 1, \dots, 24; \quad X \text{ and } Y \in \{0,1\} \quad (15)$$

226
 227 where $W_{ess}(t)$ and $W_{ess}(t-1)$ are the quantities of energy storage inside the battery at hour t and
 228 $t-1$ respectively, P_{charge} and $P_{discharge}$ are the allowed rates of charge and discharge through a
 229 definite period of time ($\Delta t = 1h$), η_{charge} and $\eta_{discharge}$ are the charge and discharge efficiency.

230
 231 **4. Imperialist competitive algorithm**
 232

233 Imperialist competitive algorithm (ICA) is a new algorithm that has been proposed by Atashpaz-
 234 Gargari and Lucas based on the human's socio political in different fields of engineering. The
 235 random initial population in this method is called countries. Some countries with the less cost are
 236 chosen to be imperialist, and the others are considered colonies of these imperialists. The countries
 237 are arrays that their dimension depends on the dimension of the optimization and each of them is
 238 defined by:

239
 240 $Country = [P_1, P_2, P_3, \dots, P_N]$ (16)

241
 242 Where, P_i are regarded as the variable values that should be optimized. The cost of each country can
 243 be found by evaluation of the cost function (f) by the following equation:

244
 245 $C_i = f(country_i) = f(P_1, P_2, P_3, \dots, P_N)$ (17)

246
 247 The algorithm begins with initial population of size N and N_{imp} is selected as the country with
 248 minimum cost in order to create the empires [32]. The remaining of the population (N_{col}) will be the
 249 colonies that each of them belongs to one of the empires.

250 For dividing amongst the imperialist, some of these colonies proportional to their power are
 251 transferred to each imperialist.

252 For proper division of the colonies amongst the imperialists, we define the normalized cost of an
 253 imperialist by:

254
 255 $C_n = \max(c_i) - c_n$ (18)

256
 257 C_n and c_n are normalized cost and cost of n-th imperialists, respectively. After determining the
 258 normalized cost of all imperialists, the normalized power of each imperialist is determined
 259 according to the following equation:

260
 261
$$P_n = \left| \frac{C_n}{\sum_{i=1}^{N_{imp}} C_i} \right|$$
 (19)

262
 263 In the other words, the normalized power of an imperialist is the part of colonies that should be
 264 possessed by that imperialist [33]. Afterward, the primary number of colonies for n-th empire will
 265 be defined by following:

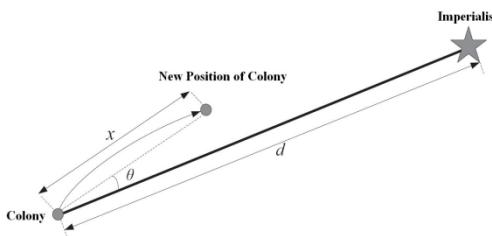
266
 267 $NC_n = round\{P_n \cdot N_{col}\}$ (20)

268
 269 Where, NC_n is primary number of colonies belonging to the n-th imperialists and N_{col} is the total
 270 number of remaining colonies in the primary countries crowds.

271 After this stage, operators of ICA must be accomplished. There are three operators in ICA:
 272 Assimilation, Exchange and Imperialistic Competition. They are exhibiting as follows:
 273

274 **4.1. Assimilation**

275 Imperialist states try to attract their colonies to move themselves toward the direction of different
 276 socio-political axis such as social welfare. This process is called assimilation policy. By moving all
 277 the colonies in the direction of the imperialist, the assimilation policy is planned in ICA. This
 278 movement is shown in Fig. 2.
 279



280
 281 **Fig. 2.** Motion of colonies toward their imperialist
 282

283 In order to search different parts around the imperialist, a random quantity of deflection is added to
 284 the direction of colony motion toward its imperialist.

285 In the above figure, x is a random variable with uniform distribution that is defined by:
 286

287 $x \sim U(0, \beta \times d)$ (21)

288 Where, β is a number between one and two and near to two. d is distance between colony and
 289 imperialist and θ is a parameter with uniform distribution.

290 $\theta \sim U(-\gamma, \gamma)$ (22)

291 Where, γ is a significance parameter that its rising causes increase in searching region around
 292 imperialist and decrease of its value brings colonies near to the vector of connection between colony
 293 and the imperialist.

294 **4.2. Exchange**

295 A colony may reach to a location with lower cost than imperialist when moving toward the
 296 imperialist. In this condition, the imperialist and the colony alter their locations. Then, the algorithm
 297 will continue with the new location of the imperialist and thus the imperialist in its new location will
 298 assimilate the colonies.

299 **4.3. Imperialistic competition**

300 It is obvious that all empires attempt to get the ownership and control the colonies of other empires.
 301 In ICA, imperialistic competition is modeled by picking one of the feeblest colonies of the feeblest
 302 empire and cause a competition among all the empires to get this colony. To begin the competition,
 303 first total power of an empire is computed.

304 The total power of an empire is influenced by the power of imperialist country, while the colonies
 305 power of an empire has a negligible effect upon the total power of that empire. The total cost of
 306 each imperialist is calculated as below:

317 $TC_n = Cost(imperialist_n) + \xi \text{ mean}\{Cost(colonies of empire_n)\}$ (23)

318
 319 In the above equation, TC_n is the total cost of the n-th impire and ξ is a number between zero and
 320 one that indicates the influence of the colonies in value of the power of each imperialist [33].
 321 After calculation of the total power of an empire, a colony of the feeblest empire is chosen and then
 322 the amount of power of each empire is found by ownership probability that is proportional to the
 323 total power of the empire. Then, the normalized total cost is determined by the following:
 324

325 $NTC_n = \max\{TC_i\} - TC_n$ (24)

326
 327 Where, TC_n is total cost n-th empire and NTC_n is the normalized cost of that n-th empire. Having the
 328 normalized total cost, the ownership probability of each empire is given by:
 329

330 $P_{pn} = \left| \frac{NTC_n}{\sum_{i=1}^{N_{imp}} NTC_i} \right|$ (25)

331
 332 Where, P_{pn} is the ownership of the n-th empire. Each empire which has greater power can take more
 333 colonies.
 334 In order to divide the mentioned colonies among the empires, vector P is formed as follows:
 335

336 $P = [P_{p1}, P_{p2}, P_{p3}, \dots, P_{pN_{imp}}]$ (26)

337
 338 Then, the vector R should be created with the same size as vector P. The arrays of this vector are
 339 random number with uniform distribution between zero and one.
 340

341 $R = [r_1, r_2, r_3, \dots, r_{N_{imp}}]$ (27)

342
 343 Then, the vector D is formed by subtracting R from P.

344
 345 $D = P - R = [P_{p1} - r_1, P_{p2} - r_2, \dots, P_{pN_{imp}} - r_{N_{imp}}]$ (28)

346
 347 Referring to vector D, it will hand the mentioned colonies to an empire so that relevant index in
 348 vector D is bigger than the others. The imperialistic competition will gradually result in a growth of
 349 the power of great empires and a decrease in the power of weaker ones. Powerless empires will
 350 disintegrate in the imperialistic competition and their colonies will be divided among other empires.
 351 For execution of ICA to performance of optimal management of RESs by a VPP, The
 352 implementation steps are summarized below:

353 Step 1: Generate initial countries, each country displaying operating cost for a 24-hour period
 354 (objective function).

355 Step 2: Sort the initial countries based on the lowest operating cost.

356 Step 3: Select the imperialist cases (the countries with the less operating cost) and divide colonies
 357 among them to contribute the empires.

358 Step 4: Move colonies toward their relevant imperialist and apply assimilation. Again, compute the
 359 objective function for each country.

360 Step 5: If a colony in an empire has lower operating cost than of imperialist, exchange the location
 361 of that imperialist and the colony.

362 Step 6: Compute the operating cost of an empire.

363 Step 7: Pick the feeblest colony from the feeblest empire and assign it to the empire that has the
 364 most probability to possess it.

365 Step 8: If there is an empire with no colony, eliminate the empire.

366 Step 9: If there is only one empire, stop condition if not, go to the step 4.

367 **5. Uncertainty modeling**

368

369 There are three main methods to consider the uncertainty effect [34, 35]: the first one is Mont Carlo
 370 Simulation (MCS) that has some defects such as complicated computation. The second one is the
 371 analytical techniques that can satisfy MCS fault, but they need some mathematical assumptions to
 372 make the problem much more easier. The third one is approximate method [36] that can overcome
 373 the defects of both previous methods. The 2m point estimate method (PEM), as an approximate
 374 method, is a proper and straightforward method to model the uncertainty in investigated problem.
 375 This paper implements the 2m PEM to model the uncertainty in market prices, load demand, and
 376 available output power of PV and WT units.

377

378 **5. 2m point estimate method**

379

380 The 2m PEM is a modified version of the original point estimate method [37]. The normal
 381 distribution function is used to model uncertain variables. With the utilization of 2m PEM, each
 382 random variable in the uncertain problem is substituted by two deterministic points on both sides of
 383 the mean value of the distribution function. Then, for each random variable, the problem is solved
 384 for above and below mean value. The mathematical formulation is as described below:

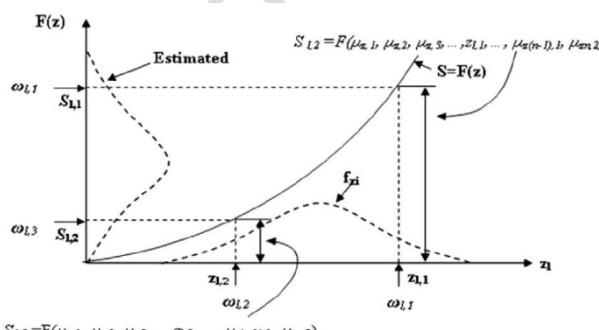
385

$$386 \quad S = F(Z) \quad (29)$$

$$387 \quad Z = [z_1, z_2, \dots, z_m]$$

388

389 Where set of input variables is shown by Z and S as output variables. In order to, for each uncertain
 390 variable (z_l), a probability function (f_{z_l}) is considered. This method utilizes three points of f_{z_l} as
 391 sample points to substitute them with two probability ones. Therefore, for m random input variables,
 392 2m PEM will solve Eq. (26) 2m times. The probabilistic description of 2m PEM is shown in Fig. 3.

393 **Fig. 3.** The conceptual idea of 2m PEM

394

395

396

397 As it is shown in the above figure, the input data $Z_{l,1}$ & $Z_{l,2}$ are mapped to the output data $S_{l,1}$ & $S_{l,2}$,
 398 respectively. Two weighting factors are supposed $\omega_{l,1}, \omega_{l,2}$ for both $S_{l,1}$ & $S_{l,2}$ estimations. The
 399 location ($Z_{l,k}$) and weighting factor ($\omega_{l,k}$) can be considered as one pair $(Z_{l,k}, \omega_{l,k})$. Here $(Z_{l,k})$ can be
 400 formulated as follows:

401

$$402 \quad Z_{l,k} = \mu_{z_l} + \xi_{l,k} \cdot \sigma_{z_l}; k=1,2 \quad (30)$$

403

404

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408 The standard location is named as $\xi_{l,k}$ in Eq. (27) can be evaluated as below:

409

$$410 \quad \xi_{l,k} = \frac{\lambda_{l,3}}{2} + (-1)^{3-k} \sqrt{m - \left(\frac{\lambda_{l,3}}{2} \right)^2}; k = 1,2 \quad (31)$$

411
412 In Eq. (28), $\lambda_{l,3}$ as the third central moments of Z_l can be computed as follows:

413
414

$$414 \quad \lambda_{l,3} = \frac{E[(Z_l - \mu_{Zl})^3]}{(\sigma_{Zl})^3} \quad (32)$$

415
416 In Eq. (29), the expected value is shown by E and Z_l is expressed as the standard deviation for
417 output data and it can be calculated as follows:

418

$$\sigma = \sqrt{Var(S_i)} = \sqrt{E(S_i^2) - [E(S_i)]^2}$$

419

$$419 \quad E(S_i^j) = \sum_{l=1}^m \sum_{k=1}^2 (\omega_{l,k} \times S_i^j(\mu_{Z1}, \mu_{Z2}, \dots, Z_{l,k}, \dots, \mu_{Zm})) \quad (33)$$

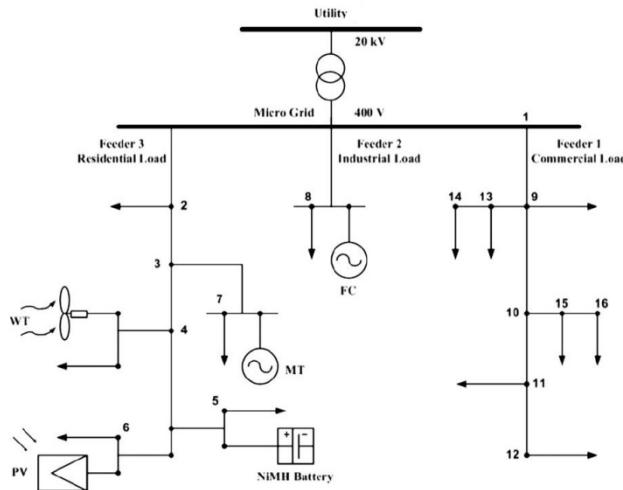
$$\omega_{l,k} = \frac{1}{2m}$$

420
421 In this paper, the uncertainty associated with the load demand forecast error, market price changes
422 and PV and WT output power changes are modeled in the problem. For example, suppose that the
423 l th load value $P_{L,l}(t)$ should be modeled by the PEM. By assuming the normal distribution function
424 for all the load amounts, the PEM will solve this problem for two times. To simulate this
425 uncertainty, it is supposed that the value of $P_{L,l}(t)$ is placed on the mean value of the load $\mu_{P_{L,l}(t)}$, then
426 after that, according to the Eq. (27), two new points are generated to replace $P_{L,l}(t)$ as
427 $Z_{l,k} = \mu_{P_{L,l}(t)} + \xi_{l,k} \sigma_{P_{L,l}(t)}$; $k = 1,2$. As it can be seen in Eq. (28), also the amount of the $\xi_{l,k}$ can be
428 calculated. The optimal management problem should be solved for two new load amounts
429 separately. Modeling the other uncertain variables can be implemented, similarly. Finally, the
430 optimal solutions are aggregated to determine the expected amount of the objective function.

431
432 **6. Simulation results**

433
434 In order to verify the effectiveness and generality of the proposed ICA for the optimal energy
435 management problem, it is implemented on a low voltage case study. This system consists of
436 several types of RESs such as WT, PV, FC, MT and also one storage device such as NIMH-Battery.
437 The single diagram of the system is shown in Fig. 4. The system complete data is extracted from
438 [30]. As it can be seen, the system includes an industrial area for the supplement of a workshop, a
439 residential area and a light commercial customer. The analysis is implemented for a 24 h time
440 interval to see the performance of each power unit better. It is assumed that all the DGs generate
441 active power at unit power factor. In addition, the heat load demand is not considered in the
442 proposed system. Moreover, there is a power exchange link between the VPP and the utility in order
443 to trade energy at any hour in the day.

444

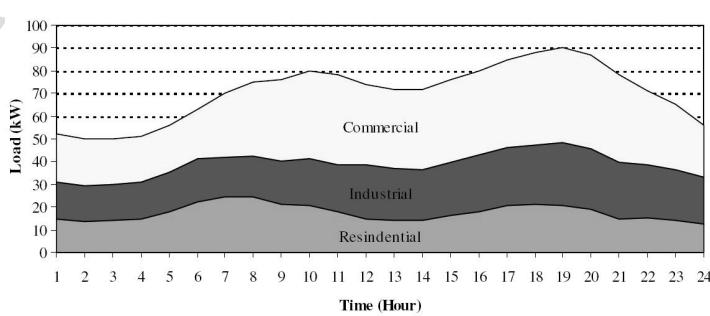


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449 Fig. 4. Single line diagram of the test system

450 The maximum and the minimum generation limit and bids information for each of the DGs are
451 shown in Table 1. As it can be seen from this table, although the WT and PV do not require any fuel
452 for power generation, their bid is higher than the other DGs. This event is because of their high
453 capital cost. The higher bid of these RESs offers to return the extra capital cost as well as to pay for
454 renewal and maintenance costs. Also the cost of startup/shut-down for each unit in cent of Euro
455 (€ct) per kilo-Watt hour (kWh) are given in Table 1. The total load demand during a 24 h time
456 interval equals 1695KW as shown in Fig. 5. The hourly forecasted market prices for the examined
457 period are considered as Table 2. The forecasted PV and WT power generation for each hour are
458 plotted in Fig. 6. In order to better understanding our study, three different scenarios are considered.
459 In the first scenario, all the DGs are dispatched regarding their real constraints. In the second
460 scenario, all DGs are allowed to start up or shut down and the battery initial charge is zero. In fact,
461 the battery should be charged in the first hours to be able to discharge at later hours and the third
462 scenario, the utility is assumed as an unconstraint unit that can exchange energy with VPP without
463 any restriction.
464
465
466

Table1
464 The limitations and bids of RESs and the utility
465
466

ID	Type	Min power (kW)	Max power (kW)	Bid (€ct/kWh)	Start up/ Shut down cost(€ct)
1	MT	6	30	0.457	0.96
2	FC	3	30	0.294	1.65
3	PV	0	25	2.584	0
4	WT	0	15	1.073	0
5	Battery	-30	30	0.38	0
6	Utility	-30	30	-	-

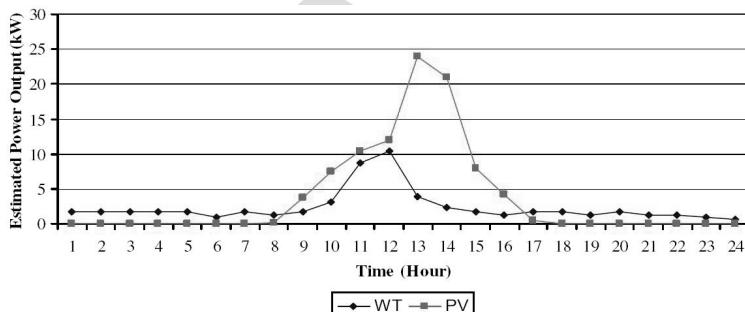


469
470
471 Fig. 5. Daily load curve of the test system

472
473
474**Table2**
The real-time market

h	Price (€ct/KWh)
1	0.23
2	0.19
3	0.14
4	0.12
5	0.12
6	0.2
7	0.23
8	0.38
9	1.50
10	4.00
11	4.00
12	4.00
13	1.50
14	4.00
15	2.00
16	1.95
17	0.60
18	0.41
19	0.35
20	0.43
21	1.17
22	0.54
23	0.30
24	0.26

475

**Fig. 6.** Forecasted power output from WT and PV476
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6.1. First scenario

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In the first scenario, it is supposed that all the units with related characteristics generate electricity and surplus of energy or additional demand inside of the grid is exchanged with the utility from the point of common coupling. All the units including the utility can operate just within their power limits while satisfying the required restrictions. The simulation results for the first scenario are presented in Table 3. As it can be seen from this table, the ICA has much better performance than the other algorithms. Comparison of results in the case of the best and the worst solutions for objective function indicates that the ICA not only demonstrates a better performance but also presents a faster convergence characteristic. The output power of the DGs in the first scenario are shown in Table 4.

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As it can be seen from this table, at the early morning hours of a day a large part of the load is supplied by the FC and the utility because their bids are lower in comparison with other DGs. Due to the increasing of demand and bids of utility during the next hours of the day, DGs increase their output powers according to priority in lower cost. It should be also noted that the battery charging

494 process has done at the first hours of the day when the prices are low but the discharge process will
 495 be done at midday when the load curve achieves peak values.

496

497 **6.2. Second scenario**

498

499 In the second scenario, the DGs can switch between the ON/OFF modes but the initial charge of the
 500 battery is zero. It means that the discharge amount of battery is limited by the amount of energy that
 501 is charged in the last hours. Table 5 shows the comparison results from the performances of the
 502 different algorithms. Similarly, the results of economic power dispatch using the proposed approach
 503 are shown in Table 6.

504

505

506

Table3
Comparison of total cost for first scenario

Type	Best solution (€ct)	Worst solution (€ct)	Mean (€ct)
GA [30]	162.9469	198.5134	179.6502
PSO[30]	162.0083	180.2282	171.2103
FSAPSO[30]	161.5561	175.5402	168.2442
CPSO-T[30]	161.0580	165.3110	162.9845
CPSO-L[30]	160.7708	163.5512	162.1614
AMPSO-T[30]	159.9244	160.4091	160.2368
AMPSO-L[30]	159.3628	159.6813	159.5143
ICA	151.4229	151.4253	151.4241

507

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509

510

Table4
Economic dispatch using ICA (first scenario)

Time (h)	DG sources					
	MT	FC	PV	WT	Battery	Utility
1	6	30	0	0	-14	30
2	6	30	0	0	-16	30
3	6	30	0	0	-16	30
4	6	30	0	0	-15	30
5	6	30	0	0	-10	30
6	6	30	0	0	-3	30
7	6	30	0	0	4	30
8	6	30	0	0	9	30
9	30	30	0	1.785	30	-15.785
10	30	30	7.528	3.09	30	-20.615
11	30	30	9.225	8.775	30	-30
12	30	30	3.59	10.41	30	-30
13	30	30	0	3.915	30	-21.915
14	30	30	9.63	2.37	30	-30
15	30	30	0	1.785	30	-15.785
16	30	30	0	1.305	30	-11.305
17	30	30	0	0	30	-5
18	6	30	0	0	30	22
19	6	30	0	0	24	30
20	6	30	0	0	30	21
21	30	30	0	1.3005	30	-13.3005
22	30	30	0	0	30	-19
23	6	30	0	0	-1	30
24	6	30	0	0	-10	30

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Table5
Comparison of total cost for second scenario

Type	Best solution (€ct)	Worst solution (€ct)	Mean (€ct)
GA [38]	334.8694	345.0211	336.2912
PSO[38]	327.7211	340.3123	331.2102
FSAPSO[38]	326.4291	335.4931	331.4301
0- PSO[38]	318.6401	332.9012	322.9102
SAM- 0- PSO [38]	299.4124	299.9012	299.4124
ICA	299.1013	299.1042	299.1027

514
515 As it can be seen Table 6, the battery is charged in the first hours of day (hours 1-8), even by buying
516 energy from MT. This event indicates that it is more economical to charge the battery by the use of
517 MT to reduce the utility power generation at later times. During the high price period (hours 9-16),
518 the battery is discharging at heavy load times to supply the utility by selling energy to it. In addition,
519 at hours 23-24 the MT is forced to decrease its power to reduce the total cost. This event leads the
520 MT to shut down at hour 24.

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Table6
Economic dispatch using ICA (second scenario)

Time (h)	DG sources					
	MT	FC	PV	WT	Battery	Utility
1	20.215	30	0	1.785	-30	30
2	18.215	30	0	1.785	-30	30
3	18.215	30	0	1.785	-30	30
4	19.215	30	0	1.785	-30	30
5	24.215	30	0	1.785	-30	30
6	30	30	0	0.915	-27.915	30
7	30	30	0	1.785	-21.785	30
8	30	30	0.2	1.305	-16.505	30
9	30	30	3.75	1.785	30	-19.535
10	30	30	7.525	3.09	30	-20.615
11	30	30	10.45	8.775	28.775	-30
12	30	30	11.95	10.41	21.64	-30
13	30	30	23.9	3.915	14.185	-30
14	30	30	21.05	2.37	18.58	-30
15	30	30	7.875	1.785	30	-23.66
16	30	30	4.225	1.305	30	-15.53
17	30	30	0.55	1.785	-7.335	30
18	30	30	0	1.785	-3.785	30
19	30	30	0	1.302	-1.302	30
20	30	30	0	1.785	-4.785	30
21	30	30	0	1.3005	30	-13.3005
22	30	30	0	1.3005	0.232	9.4675
23	6	30	0	0.915	-1.915	30
24	0	30	0	0.615	-4.615	30

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530 **6.3. Third scenario**

531

532 In this scenario, it's assumed that all DGs act within their power limits but the utility behaves as an
 533 unconstraint unit and exchanges energy with the VPP without any restriction. Similar to the
 534 previous cases, the comparison results of performances are implemented to solve the economic
 535 dispatch problem and the simulation results are gathered correspondingly as shown in Table 7. The
 536 best optimal power dispatch using ICA for a day ahead and in terms of cost objective is also
 537 tabulated in Table 8.

538

539

540

Table7
Comparison of total cost for third scenario

Type	Best solution (€ct)	Worst solution (€ct)	Mean (€ct)
GA [30]	91.3293	127.7625	105.2070
PSO[30]	90.7629	112.8628	99.8493
FSAPSO[30]	90.6919	108.7761	99.7340
CPSO-T[30]	90.5545	102.1001	96.3273
CPSO-L[30]	90.4833	100.8786	95.6809
AMPSO-T[30]	89.9917	90.6221	90.3119
AMPSO-L[30]	89.9720	90.0431	90.0080
ICA	65.8273	65.8284	65.8295

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Table8
Economic dispatch using ICA (third scenario)

Time (h)	DG sources					
	MT	FC	PV	WT	Battery	Utility
1	6	3	0	0	-30	73
2	6	3	0	0	-30	71
3	6	3	0	0	-30	71
4	6	3	0	0	-30	72
5	6	3	0	0	-30	77
6	6	3	0	0	-30	84
7	6	4	0	0	-30	90
8	6	30	0	0	-30	69
9	30	30	0	1.7855	30	-15.7855
10	30	30	7.5279	3.0854	30	-20.6133
11	30	30	10.4412	8.7724	30	-31.2136
12	30	30	11.964	10.413	30	-38.377
13	30	30	0	3.9228	30	-21.9228
14	30	30	21.0493	2.3766	30	-41.4259
15	30	30	0	1.7855	30	-15.7855
16	30	30	0	1.3017	30	-11.3017
17	30	30	0	0	30	-5
18	6	30	0	0	30	22
19	6	30	0	0	-30	84
20	6	30	0	0	30	21
21	30	30	0	1.3017	30	-13.3017
22	30	30	0	0	30	-19
23	6	30	0	0	-30	59
24	6	3	0	0	-30	77

547 As it can be seen Table 8, the utility takes the lead in supplying the load inside the grid during the
 548 first hours of the day while purchasing energy in large quantities from the VPP during the peak
 549 times. Regarding objective function, PV and WT start-up when shortage of power generation
 550 happens inside the grid or there is a need for more energy to the utility. The other DG units such as
 551 FC and storage battery generate electricity at their maximum rates during the most hours of the day
 552 while MT holds the maximum power level during a period of time from 9-17.

553

554 7. Conclusion

555

556 In this paper, an ICA method is introduced and applied to solve the optimal management of RESs
 557 such as WT, PV, FC and MT and one storage device like a battery that 2m PEM was implemented
 558 to cover the uncertainties in load demand, market price and available output power of the WT and
 559 PV units for a 24 h time interval. To investigate the performance of the proposed algorithm three
 560 different scenarios have been proposed and the simulation results in each scenario have been
 561 collected truly. The numerical results showed that proposed optimization method reduced the
 562 operation cost fairly well in comparison to the other methods.

563

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- 1- Integrated operation of wind turbine, photovoltaic panel, fuel cell, micro turbine, energy storage systems and controllable loads by virtual power plant.
- 2- Consider uncertainties related to forecasted values for load demand, market price, output power of wind and photovoltaic.
- 3- Investigating the application of methodology to reduce the operational cost with considering energy loss cost under three scenarios for a 24-hour period.
- 4- Optimal management is formulated by one optimization meta-heuristic algorithm, Imperialist Competitive Algorithm (ICA).